

Comparison of Basic Inductive Power Transfer Systems with Linear Control Achieving Optimized Efficiency

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Abstract—Inductive power transfer (IPT) systems with front-side and load-side converters are generally developed for better overall system efficiency than a single IPT converter by providing maximum efficiency tracking and output regulation against variations of coupling coefficient (k) and load. The optimum efficiency point of an IPT converter is at a particular loading resistance, which varies with k and is hard to measure directly for the purpose of control. Perturb and observe (P&O) control is normally implemented to iteratively track the optimum efficiency point. However, this heuristic algorithm results in slow response to the variations of k and load. Recently, a much faster linear control for optimum efficiency tracking has been developed for the series-series (SS) IPT system only. This paper proposes a general linear control scheme for all four basic IPT systems to track the optimum efficiency point. Unlike the SS IPT converter, it is found that additional control of either frequency or adaptive compensation is needed for the other three basic IPT converters to operate against the variation of k . Different input to output transfer functions and their k - and load-independent properties at optimum efficiency are identified for all four basic IPT systems. Thus, a general fast linear control can be applied in the front-side converter to achieve optimum efficiency, while the load-side converter regulates the output power independently. Furthermore, the maximum efficiencies of the IPT converters with these four basic compensations for an identical loosely-coupled transformer are compared theoretically and verified experimentally. The parallel-parallel IPT converter gives the best efficiency. Its additional frequency control in conjunction with the optimum efficiency tracking and the output power regulation is also experimentally validated.

Index Terms—Inductive power transfer, linear control, optimized efficiency, comparison.

I. INTRODUCTION

Inductive power transfer (IPT) systems have found many applications in wireless charging of portable electronic devices [1]–[4], roadway-powered electric vehicles [5]–[9] and biomedical implants [10]–[12]. IPT converters inevitably contain loosely-coupled transformers in order to allow power to be transmitted wirelessly between the primary and secondary windings. The large leakage inductance of the transformer must be compensated using external capacitors and/or inductors in order to achieve near zero reactive power so that the power rating and loss from the power driver can be substantially minimized [13], [14]. The basic IPT converters contain minimal number of external compensation components, i.e.,

two capacitors, one at each side of the transformer windings. The connections can be in series or parallel. Thus, four basic IPT converters can be identified according to the primary-secondary compensation types, namely, series-series (SS), series-parallel (SP), parallel-series (PS), and parallel-parallel (PP) IPT converters. Once compensated, an IPT converter behaves as a resonant converter with the maximum efficiency occurring at a very narrow vicinity of an optimal operating point [15]. When the operating point deviates slightly from the optimal point, the converter efficiency drops significantly.

To maintain the IPT converter at its optimal operating point for applications with large variations of coupling coefficient (k) and load, maximum efficiency tracking (MET) has been widely studied. In [16], a load-side converter cascaded to an SS IPT converter is used to adaptively emulate an optimal load. However, no regulation of the load power is provided by the load-side converter. Improved IPT systems with MET algorithms have been proposed. The improved system has a front-side converter (or the internal inverter of the IPT converter) controlled to maximize the efficiency (or minimize the input power), while the load-side converter is responsible for the regulation of the output power against load change [17]–[23].

Typical MET algorithms are based on an iterative computer algorithm called “perturb and observe” (P&O) [16]–[23]. The P&O algorithm inevitably has to balance between a sufficiently small steady-state error and an acceptable dynamic response by choosing a suitable incremental value of the control variable. In these IPT systems, the slow iterative process of the P&O algorithm often results in poor dynamic response to the variations of k and load. Furthermore, it may cause large overshoot/undershoot due to some seriously-mismatched-load conditions during the iterative process. In [22], with an improved sliding mode controller, the load-side converter is more adaptive to the slow response of the iterative process of P&O. However, IPT systems with P&O and sliding mode control, to a less extent, still suffer from seriously-mismatched-load conditions. Since the maximum efficiency point occurs at a specific value of the modulation index for controlling the power of the IPT converter, an iterative algorithm for maximum efficiency tracking is still a necessary. Nonetheless, a non-iterative controller is desired. Fortunately, maximum efficiency is found to be at a specific voltage transfer ratio of the SS IPT converter designed at its optimal operating point with a load-independent transconductance and an input zero phase angle (ZPA) such that the relationship between the modulation index and the voltage transfer ratio is

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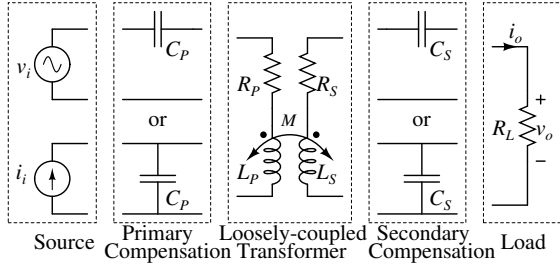


Fig. 1. Essential building blocks of a basic IPT converter.

monotonic, thus allowing a linear controller to be developed [24]. The linear controller for the SS IPT converter has been proved to have a much faster response and smaller steady-state error in keeping the system at its maximum efficiency against the variations of k and load. However, the linear maximum efficiency controller is only available for SS IPT systems. Linear controllers for maximum efficiency operation of all four basic IPT converters and their efficiency comparisons are still missing.

In this paper, conditions for achieving load-independent transfer function and ZPA will be highlighted for all four basic IPT converters. Additional requirements of frequency or compensation control are illustrated for the optimum operations of SP, PS and PP IPT converters against variation of k . Control references of transfer functions at maximum efficiency points of these IPT converters are derived for maximum efficiency control. The linear control scheme proposed in [24] can therefore be applied in these IPT systems for achieving efficiency optimization against the variations of k and load. A comparison of maximum achievable efficiency for these four basic IPT converters taking into consideration losses from practical converters will be given. This paper presents a generalization of the research work in [24] to cover all basic IPT converter systems.

This paper is organized as follows. Section II introduces the four basic IPT converters and derives the optimum operating points for achieving load-independent output, maximum efficiency and ZPA. In Section III, control references at the optimum operating points are derived for the linear controllers. Section IV compares power efficiencies of practical systems using the four basic compensations. Section V elaborates the linear control scheme for achieving maximum efficiency with output regulation against the variation of k . Experimental verifications are given in Section VI. Finally, Section VII concludes this paper.

II. OPTIMAL EFFICIENCY OPERATING POINT OF AN IPT CONVERTER MODEL

A. Basic IPT Converter

Fig. 1 shows some essential building blocks of a basic IPT converter model, where the loosely-coupled transformer has self inductances L_P and L_S , and a mutual inductance M . As usual, the coupling coefficient k is defined as $\frac{M}{\sqrt{L_P L_S}}$. Unless indicated otherwise, subscripts P and S indicate parameters on the primary and secondary sides, respectively.

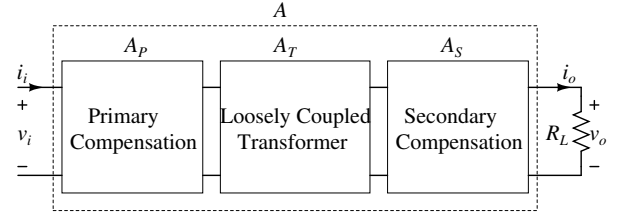


Fig. 2. Schematic of an IPT converter as a two-port network.

TABLE I
MATRIX OF SUBNETWORKS

	Series Compensation	Parallel Compensation
A_P	$\begin{bmatrix} 1 & \frac{1}{j\omega C_P} \\ 0 & 1 \end{bmatrix}$	$\begin{bmatrix} 1 & 0 \\ j\omega C_P & 1 \end{bmatrix}$
A_S	$\begin{bmatrix} 1 & \frac{1}{j\omega C_S} \\ 0 & 1 \end{bmatrix}$	$\begin{bmatrix} 1 & 0 \\ j\omega C_S & 1 \end{bmatrix}$
A_T	$\begin{bmatrix} \frac{j\omega L_P + R_P}{j\omega M} & \frac{1}{j\omega M} \end{bmatrix}$	$\begin{bmatrix} j\omega M(\frac{1}{k^2} - 1) + \frac{R_P R_S + j\omega L_P R_S + j\omega L_S R_P}{j\omega M} & \frac{j\omega L_S + R_S}{j\omega M} \end{bmatrix}$

Using this transformer model, losses are modeled aggregately using equivalent resistors R_P and R_S as described in [25], [26]. Resistor R_P includes losses from the primary windings and the inverter circuit. Resistor R_S includes losses from the secondary windings and the rectifier circuit. External capacitors C_P and C_S are used to compensate the loosely-coupled transformer in either series or parallel connection. They resonate with self inductances at frequencies $\omega_P = \frac{1}{\sqrt{L_P C_P}}$ and $\omega_S = \frac{1}{\sqrt{L_S C_S}}$. For an appropriate primary-side compensation, an IPT converter with primary series compensation is mostly driven by an equivalent AC voltage source v_i , while an IPT converter with primary parallel compensation is mostly driven by an equivalent AC current source i_i . Normally, either output voltage v_o or output current i_o is regulated conveniently for the required output power. In this way, we can have two output transfer functions for each type of power source. For voltage input, the transfer functions are a voltage gain $\frac{v_o}{v_i}$ and a transconductance $\frac{i_o}{v_i}$. Likewise, for current input, the transfer functions are a transresistance $\frac{v_o}{i_i}$ and a current gain $\frac{i_o}{i_i}$. The power regulation for MET will need the control of both transfer functions. It can be enhanced by designing one of the two transfer functions to achieve a load-independent output. With this load-independent design, the two transfer functions are polarized and targeting to be either completely load-independent or completely load-dependent.

B. Two-port Network Model

The schematics of IPT converters shown in Fig. 1 can be simplified using two-port networks [27], as shown in Fig. 2. The two-port networks are represented by

$$[v_i, i_i]^T = A[v_o, i_o]^T, \quad (1)$$

where $A = A_P A_T A_S$ is the product of the gains of primary compensation A_P , loosely-coupled transformer A_T and secondary compensation A_S . The details of subnetworks are given in Table I. As two-port network A only consists of linear

TABLE II
EXPRESSIONS OF TRANSFER FUNCTIONS, INPUT IMPEDANCE AND EFFICIENCY

Topologies	G	Z_{in}	η
SS	$\frac{i_o}{v_i} = \frac{j\omega M}{Z_P Z_{S-S} + \omega^2 M^2}$	$Z_P + \frac{\omega^2 M^2}{Z_{S-S}}$	$\frac{\omega^2 M^2 R_L}{ Z_{S-S} ^2 R_P + \omega^2 M^2 (R_L + R_S)}$
PS	$\frac{i_o}{i_i} = \frac{\frac{M}{C_P}}{Z_P Z_{S-S} + \omega^2 M^2}$	$\frac{Z_P - \frac{1}{j\omega C_P} + \frac{\omega^2 M^2}{Z_{S-S}}}{j\omega C_P (Z_P + \frac{\omega^2 M^2}{Z_{S-S}})}$	
SP	$\frac{v_o}{v_i} = \frac{j\omega M \frac{R_L}{j\omega C_S R_L + 1}}{Z_P Z_{S-P} + \omega^2 M^2}$	$Z_P + \frac{\omega^2 M^2}{Z_{S-P}}$	$\frac{\omega^2 M^2 \frac{R_L}{1 + \omega^2 C_S^2 R_L^2}}{ Z_{S-P} ^2 R_P + \omega^2 M^2 (\frac{R_L}{1 + \omega^2 C_S^2 R_L^2} + R_S)}$
PP	$\frac{v_o}{i_i} = \frac{\frac{M}{C_P} \frac{R_L}{j\omega C_S R_L + 1}}{Z_P Z_{S-P} + \omega^2 M^2}$	$\frac{Z_P - \frac{1}{j\omega C_P} + \frac{\omega^2 M^2}{Z_{S-P}}}{j\omega C_P (Z_P + \frac{\omega^2 M^2}{Z_{S-P}})}$	
$Z_P = j\omega L_P + R_P + \frac{1}{j\omega C_P}$, $Z_{S-S} = j\omega L_S + R_S + \frac{1}{j\omega C_S} + R_L$ and $Z_{S-P} = j\omega L_S + R_S + \frac{R_L}{j\omega C_S R_L + 1}$.			

TABLE III
ADDITIONAL CONTROL REQUIREMENT FOR THE VARIATION OF k

Topologies	Adaptive Compensation	Frequency Tracking
SS	Nil	Nil
SP	Required	Nil
PS	Required	Nil
PP	Nil	Required

passive inductors, capacitors, and parasitic resistors, it is a reciprocal network. Define

$$A = \begin{bmatrix} a_{11} & a_{12} \\ a_{21} & a_{22} \end{bmatrix}, \quad (2)$$

and by the principle of reciprocity, we have

$$a_{11}a_{22} - a_{12}a_{21} = 1, \quad (3)$$

and

$$\begin{bmatrix} v_i \\ i_i \end{bmatrix} = A \begin{bmatrix} v_o \\ i_o \end{bmatrix} = \begin{bmatrix} a_{11} & a_{12} \\ a_{21} & a_{22} \end{bmatrix} \begin{bmatrix} v_o \\ i_o \end{bmatrix}. \quad (4)$$

Obviously from Fig. 2, we also have $v_o = i_o R_L$.

Load-independent transfer functions have been studied previously for the SS, SP and PP IPT converters [25], [26], [28]. It is found that for an efficiency-optimized design, the SS and PS IPT converters should achieve load-independent current (LIC) output while the SP and PP IPT converters should achieve load-independent voltage (LIV) output. From (3) and (4), the transfer functions of the four IPT converters are readily given by

$$G = \begin{cases} \frac{i_o}{v_i} = \frac{1}{a_{11}R_L + a_{12}}, & \text{for SS,} & (5a) \\ \frac{v_o}{v_i} = \frac{1}{a_{11} + \frac{a_{12}}{R_L}}, & \text{for SP,} & (5b) \\ \frac{i_o}{i_i} = \frac{1}{a_{21}R_L + a_{22}}, & \text{for PS, and} & (5c) \\ \frac{v_o}{i_i} = \frac{1}{a_{21} + \frac{a_{22}}{R_L}}, & \text{for PP} & (5d) \end{cases}$$

IPT converters. The conditions of load-independent outputs for SS, SP, PS and PP IPT converters are $a_{11} = 0$ in (5a), $a_{12} = 0$ in (5b), $a_{21} = 0$ in (5c) and $a_{22} = 0$ in (5d), respectively.

From (4), the input impedance of these IPT converters is given by

$$Z_{in} = \frac{v_i}{i_i} = \frac{a_{11}R_L + a_{12}}{a_{12}R_L + a_{22}}. \quad (6)$$

To achieve ZPA between v_i and i_i , Z_{in} should have no imaginary component, i.e.,

$$\Re(Z_{in}) = Z_{in}. \quad (7)$$

In this paper, $\Re$ and $\Im$ represent the calculation of real component and imaginary component, respectively.

The power efficiency of the four IPT converters can be calculated from

$$\eta = \frac{\Re(v_o i_o)}{\Re(v_i i_i)}. \quad (8)$$

Table II gives a summary of expressions before optimization of transfer function G , input impedance Z_{in} and efficiency η for the four basic IPT converters. These expressions will be optimized at an operating frequency for the desired load-independent transfer function and input zero phase angle.

C. Load-independent Transfer Functions with Zero Phase Angle

For a practical IPT converter, R_P and R_S are non-zero and thus a perfect load-independent transfer function is not possible. However, a near perfect load-independent transfer function can be obtained by assuming $R_P = 0$ and $R_S = 0$. With the conditions to achieve load-independent output and ZPA discussed in Section II-B [25], [26], [28], ideal load-independent transfer function $|G_i|$ is given by

$$\left| \frac{i_o}{v_i} \right| = \frac{1}{\omega_P M}, \quad \text{for SS,} \quad (9a)$$

$$\left| \frac{v_o}{v_i} \right| = \frac{L_S}{M}, \quad \text{for SP,} \quad (9b)$$

$$\left| \frac{i_o}{i_i} \right| = \frac{L_P}{M}, \quad \text{for PS, and} \quad (9c)$$

$$\left| \frac{v_o}{i_i} \right| = \omega_S M \frac{\sqrt{1-k^2}}{k^2}, \quad \text{for PP} \quad (9d)$$

compensated IPT converters, at an operating frequency ω , given by

$$\omega = \begin{cases} \omega_P = \omega_S, & \text{for SS,} & (10a) \\ \omega_S = \frac{\omega_P}{\sqrt{1-k^2}}, & \text{for SP,} & (10b) \end{cases}$$

$$\omega = \begin{cases} \omega_P = \frac{\omega_S}{\sqrt{1-k^2}}, & \text{for PS, and} & (10c) \end{cases}$$

$$\frac{\omega_P}{\sqrt{1-k^2}} = \frac{\omega_S}{\sqrt{1-k^2}}, \quad \text{for PP} \quad (10d)$$

compensated IPT converters. From (10), ω , ω_P or ω_S may vary with k as a consequence of misalignment or variation of the gap distance of the loosely coupled transformer. Thus, frequency control is needed for PP IPT converter and adaptive compensation is needed for SP and PS IPT converters to satisfy (10) when k varies. A summary is shown in Table III.

D. Optimal Load

The expressions of η in Table II are obtained by omitting the small equivalent series resistance of the compensation capacitors. The optimal loading resistance $R_{L,m}$ that achieves maximum efficiency can be obtained by putting ω from (10) into η in Table II, and solving $\frac{d\eta}{dR_L} = 0$ for $R_{L,m}$ which is approximately given by

$$R_{L,m} \approx \begin{cases} \omega_P M \gamma, & \text{for SS,} \\ \omega_S M \frac{L_S^2}{M^2} \frac{1}{\gamma}, & \text{for SP,} \\ \omega_P M \gamma, & \text{for PS, and} \\ \omega_S M \sqrt{1 - k^2} \frac{L_S^2}{M^2} \frac{1}{\gamma}, & \text{for PP} \end{cases} \quad (11a)$$

$$(11b)$$

$$(11c)$$

$$(11d)$$

compensated IPT converters, where

$$\gamma = \sqrt{\frac{R_S}{R_P}} \quad (12)$$

with assumptions

$$\frac{\omega^2 M^2}{R_P R_S} \gg 1, \text{ and} \quad (13)$$

$$\frac{1}{k^2} \gg \frac{L_P R_S}{L_S R_P} \gg k^2. \quad (14)$$

From (11), $R_{L,m}$ is k -dependent and difficult to be measured directly and accurately for operation at maximum efficiency. Therefore, a slow but universal P&O control algorithm is commonly used for the tracking of maximum efficiency or its equivalent directly.

III. k -INDEPENDENT MAXIMUM EFFICIENCY TRANSFER POINT

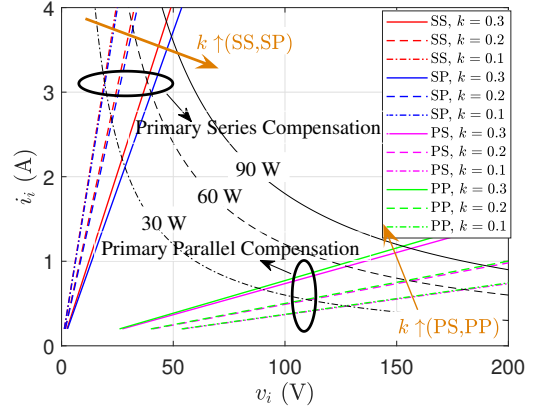
With the operating frequency given by (10), (9) gives the load-independent transfer function G_i , and (11) gives the load $R_{L,m}$ for optimal efficiency of the four basic IPT converters. As discussed in Section II-A, we have two transfer functions for the power control. The load-independent transfer function has been highlighted in Section II-C. The other transfer function should be load-dependent. It is defined as $H(R_L)$. At maximum efficiency point, we have $R_L = R_{L,m}$. Moreover, it is approximately given by

$$H(R_{L,m}) \approx \begin{cases} \left| \frac{v_o}{v_i} \right| = \gamma, & \text{for SS,} \\ \left| \frac{i_o}{v_i} \right| = \frac{1}{\omega_S L_S} \gamma, & \text{for SP,} \\ \left| \frac{v_o}{i_i} \right| = \omega_P L_P \gamma, & \text{for PS, and} \\ \left| \frac{i_o}{i_i} \right| = \frac{L_P}{L_S} \gamma, & \text{for PP} \end{cases} \quad (15a)$$

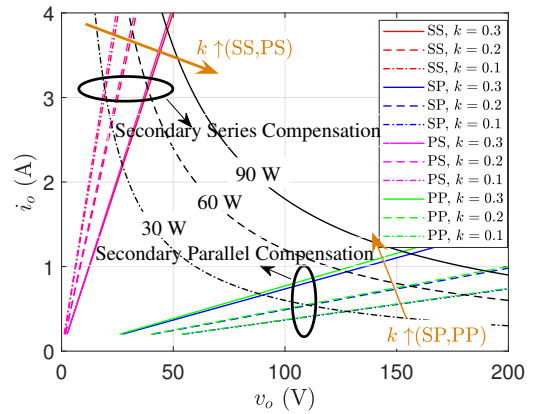
$$(15b)$$

$$(15c)$$

$$(15d)$$



(a) SS and SP IPT converters have a much higher inverter driving current.



(b) SS and PS IPT converters have a much higher diode rectifier driving current.

Fig. 3. V-I characteristics of SS, SP, PS and PP IPT converters under different values of coupling coefficient k . The long arrows indicate the direction of line moving in response to an increase of k .

compensated IPT converters. Equation (15a) has been obtained previously in [24]. In this paper, it can be observed from (15) that $H(R_L)$ at $R_L = R_{L,m}$ is k - and load-independent for all four basic IPT converters. Therefore, it is possible to operate all basic IPT converters at maximum efficiency by controlling the output according to transfer function $H(R_{L,m})$, against the variations of k and load.

IV. COMPARISON OF MAXIMUM PRACTICAL EFFICIENCY OF THE FOUR BASIC IPT CONVERTERS

It is well known that the maximum efficiencies of the four basic IPT converters using the model shown in Fig. 1 are basically identical and increase with increasing k and the quality factors of the primary or secondary windings of the IPT transformer [15]. In this section, we will compare the maximum efficiency of the four basic IPT converters when the losses from the source-side inverter and the load-side diode rectifier are taken into consideration. Inverter loss includes conduction loss and switching loss. Switching loss can be minimized by zero voltage switching for MOSFET or zero current switching for IGBT inverter switches. Conduction loss

increases with increasing current. For a given power level, higher resistance driving gives less loss for the inverter circuit. Output rectifier loss is mainly due to forward voltage drop. Therefore, higher rectifier loss is expected for higher rectifier current and lower output voltage. Similarly, higher resistance driving gives less loss for the diode-bridge circuit.

The input impedance at optimal load, defined as $Z_{in,m}$, can be calculated using (10) and (11). Since a small $\Im(Z_{in,m})$ is sufficient for soft switching, the inverter is mainly driving a resistive load with resistance given by

$$\Re(Z_{in,m}) = \begin{cases} \omega_P M \frac{1}{\gamma} & \text{for SS,} \\ \omega_P M \frac{1}{\gamma} \frac{1}{\sqrt{1-k^2}} & \text{for SP,} \\ \omega_P M \gamma \frac{L_P^2}{M^2} & \text{for PS, and} \\ \omega_P M \gamma \frac{L_P^2}{M^2} \sqrt{1-k^2} & \text{for PP} \end{cases} \quad (16a)$$

$$(16b)$$

$$(16c)$$

$$(16d)$$

compensated IPT converters.

For illustration, simulations are conducted with parameters given as follows: $L_P = L_S = 120 \mu\text{H}$, $R_P = R_S = 0.5 \Omega$. A nominal frequency is defined as $\frac{\omega_{nom}}{2\pi} = 55 \text{ kHz}$, $\omega = \omega_P = \omega_S = \omega_{nom}$ for the SS IPT converter, $\omega = \frac{\omega_P}{\sqrt{1-k^2}} = \omega_S = \omega_{nom}$ for the SP IPT converter, and $\omega = \omega_P = \frac{\omega_S}{\sqrt{1-k^2}} = \omega_{nom}$ for the PS IPT converter, and $\omega = \frac{\omega_P}{\sqrt{1-k^2}} = \frac{\omega_S}{\sqrt{1-k^2}} = \frac{\omega_{nom}}{\sqrt{1-k^2}}$ for the PP IPT converter. Unless specified otherwise, the parameters will be used for the rest of this paper.

According to the simulation parameters, the input and output V-I characteristics of the IPT converters are given in Fig. 3(a) and Fig. 3(b) by using (16) and (11), respectively. It can be observed that given a power, the current of parallel compensation of an IPT converter is much lower than that of series compensation. Thus, higher inverter and diode rectifier losses are expected for series compensated IPT converters. The losses are decreasing for series compensated windings but increasing for parallel compensated windings of the IPT converter with increasing k nevertheless. It is therefore expected that an IPT transformer compensated for the four basic IPT converters will have their own values of R_P and R_S described by the model as shown in Fig. 1.

V. CONTROL SCHEME

The IPT converters should be maintained at optimized efficiency according to (10) against the variation of k , and (11) against variation of load. To satisfy (10), frequency control and/or adaptive compensation may be needed within the IPT converter. Once (10) is satisfied, (9) and the inverter input ZPA will be automatically fulfilled for the easy implementation of linear control to satisfy (11). The extra control freedom offered by a multi-stage IPT system, as shown in Fig. 5, is often used for efficiency optimization in satisfying (11). The multi-stage IPT system includes a front-side DC-DC converter, an IPT converter and a load-side DC-DC converter. In this paper, the load-side DC-DC converter is responsible for the regulation of output voltage V_O . The front-side DC-DC converter is responsible for achieving the load impedance given by (11).

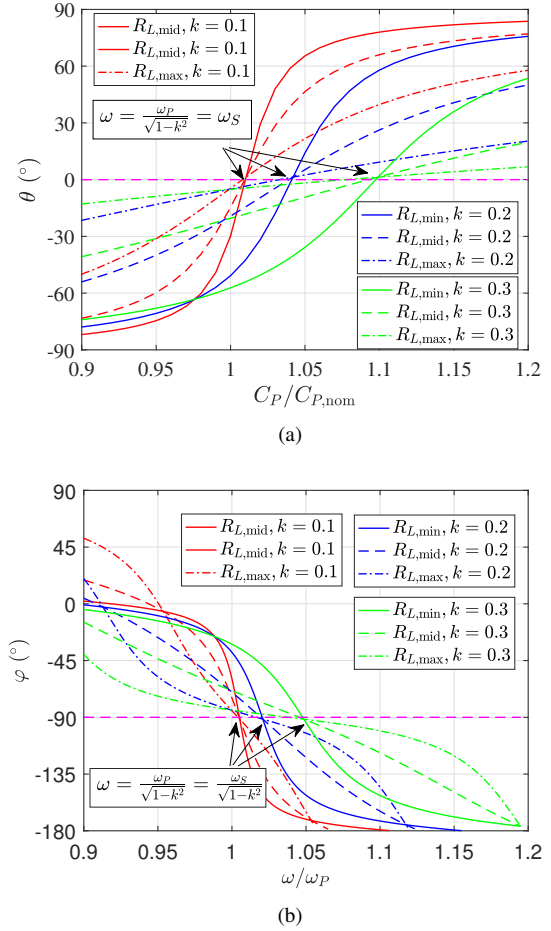


Fig. 4. (a) Input phase angle versus primary compensation capacitance of SP IPT converter. (b) Output phase angle versus operating frequency of PP IPT converter.

A. Control for Adaptive Compensation and Frequency Tracking

To operate against the variation of k , control using adaptive compensation is needed for the SP and PS IPT converters, while control using frequency tracking is needed for the PP IPT converter as summarized in Table III of Section II-C. These controls can be implemented using the phase-locked loop (PLL) based control in [29], [30].

Simulation results of input phase angle defined as $\theta = \arctan(\Im(Z_{in})/\Re(Z_{in}))$ versus compensation capacitance of the SP IPT converter are shown in Fig. 4(a). When the SP IPT converter operates at conditions given in (10b), i.e., $\omega = \omega_S = \frac{\omega_P}{\sqrt{1-k^2}}$, θ is zero and independent of k . Moreover, θ has a monotonic relationship with the compensation capacitance C_P . Therefore, a PLL controller can be used to nullify the input phase angle by tuning the compensation capacitance. Compensation capacitance can be tuned by using a switching capacitor circuit [31]–[33]. Similar control scheme can also be implemented for the PS IPT converter.

In Fig. 4(b), $\varphi = \arctan(\Im(\frac{v_o}{i_i})/\Re(\frac{v_o}{i_i}))$ is the output phase angle between the secondary output voltage v_o and the primary input current i_i for the PP IPT converter. When the PP IPT converter operates at condition (10d), φ is constant

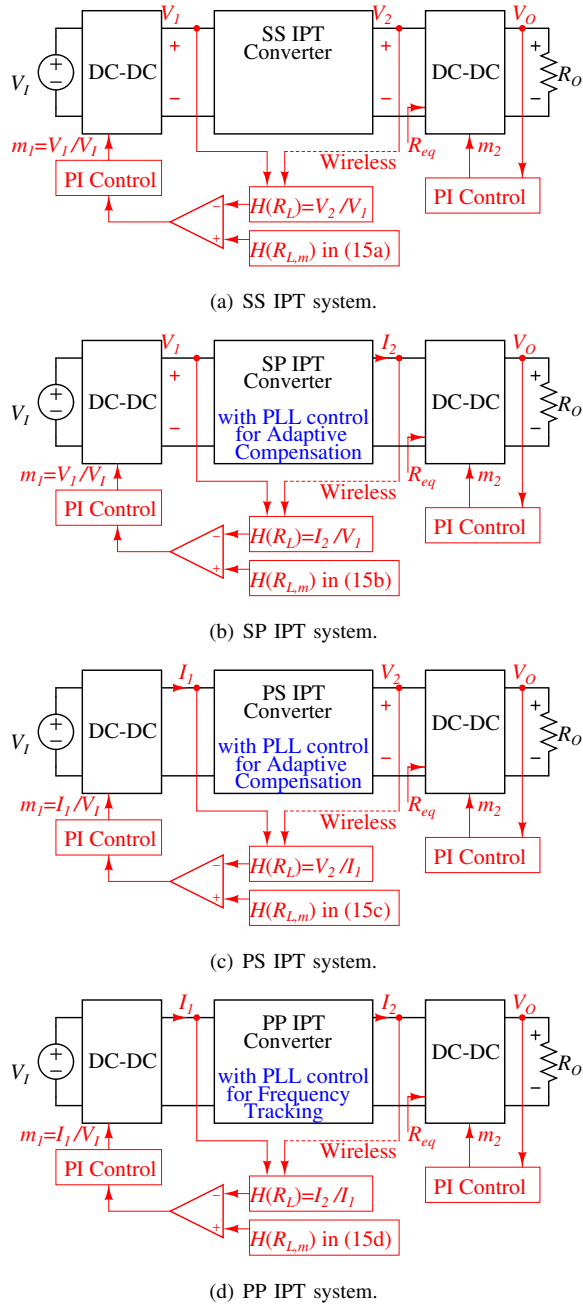
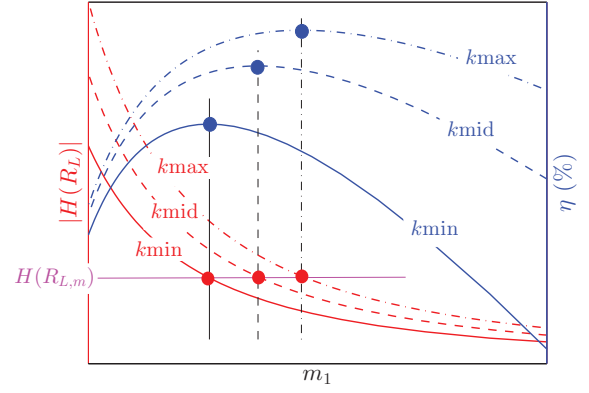


Fig. 5. Control diagrams of the three-stage IPT systems.

at -90° and independent of k . Moreover, φ has a monotonic relationship with the operating angular frequency ω . Therefore, a PLL controller can be used for frequency tracking.

B. Control for Optimized Efficiency and Output Regulation

The load-side converter regulates the output voltage V_O , so that the load appears as a constant power load P_O at the output of the IPT converter. When using a front-side pulse width modulation (PWM) converter, V_1 or I_1 is the modulated output of V_{IN} with modulation index m_1 given by $m_1 = \frac{V_1}{V_I}$ or $m_1 = \frac{I_1}{I_I}$. The equivalent load resistance R_L , as shown in Fig. 1, of the IPT converter is scaled from R_{eq} at the input of the load-side converter. Since the switching frequency of

Fig. 6. Transfer function $H(R_L)$ and efficiency η versus control variable m_1 .

the resonant circuit is much higher than the variation speed of R_{eq} , which is controlled within a much lower bandwidth in the controller of the load-side converter, R_L is considered as a slowly varying DC resistor to the resonant circuit. The scaling factor is shown in Fig. 7. Since the input of the load-side converter is a near constant power sink, its input resistance can be adjusted by varying either load-independent output V_2 or I_2 . By controlling m_1 , R_L is controlled to its optimal value $R_{L,m}$. Thus, the IPT converters can achieve their maximum efficiencies.

Modulation index m_1 has been utilized by some P&O controllers to track the maximum efficiency point. However, the dynamic response of the controller can be slow against the variations of k or load, drifting R_{eq} far away from its optimal value. Therefore, the output voltage or current of the IPT converter can be significantly overshoot or undershoot in response to the variations of k or load. It is a challenge for the design and control of the load-side converter. It has shown in [24] that using a linear PI controller to track the maximum efficiency point has advantages of faster transient response and zero steady-state error against the variations of k and load. Therefore, this paper is a generalization of the technique presented in [24] for achieving optimized efficiency for all four basic IPT converters.

As an illustration, monotonic curves of transfer function $H(R_L)$ versus control variable m_1 for various values of k are shown in Fig. 6. We observe that when the IPT converter operates at its maximum efficiency, the value of $H(R_L)$ is constant at $H(R_{L,m})$. Therefore, transfer functions $H(R_{L,m})$ calculated at $R_{L,m}$ in (15) can be a control reference for achieving maximum power efficiency [24].

In practical applications, a DC input (voltage V_1 or current I_1) and a DC output (voltage V_2 or current I_2) are measured to generate the DC transfer function for feedback control according to the type of the IPT converter shown in Fig. 5. Wireless communication is necessary to transmit information of the DC output (voltage V_2 or current I_2). Neglecting higher-order harmonics, the optimized DC transfer function is identical to the magnitude of AC transfer function. Therefore, $H(R_{L,m})$ in (15) is the control reference, as shown in Fig. 5. With a proper design, simple linear PI controllers can be

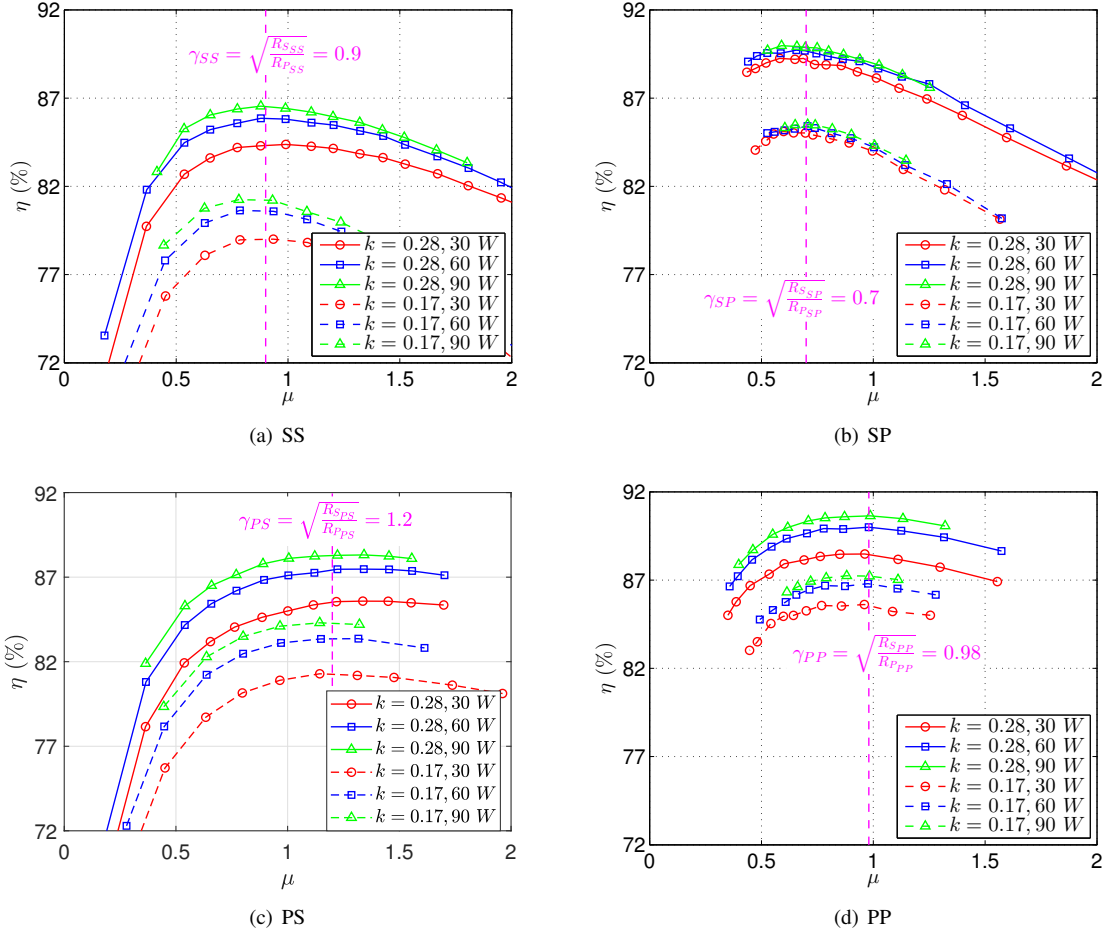


Fig. 9. Efficiency versus $\mu = \frac{\gamma H(R_L)}{H(R_{L,m})}$ for different values of coupling coefficient and load power. Vertical dash lines indicate the maximum efficiency points with a direct readout of γ .

Therefore, these fixed value transfer functions can be used as control references for achieving maximum efficiency.

B. Comparison of Maximum Efficiency Points of the Four Basic IPT Converters

The comparison of maximum efficiency is based on the system illustrated in Fig. 5. The IPT transformer is designed and optimized under some physical constraints. This transformer is used for the four basic compensations for the determination of best efficiency.

From Fig. 9, the ratio after taking square is given by $\left(\frac{\gamma_{SS}}{\gamma_{PS}}\right)^2 = \frac{R_{SSS}R_{PPS}}{R_{PSS}R_{SPS}}$, where R_{SPS} and R_{SSS} are roughly identical due to the same secondary circuitry. Thus, $\frac{R_{PPS}}{R_{PSS}} \approx \left(\frac{\gamma_{SS}}{\gamma_{PS}}\right)^2 = 0.5625$. We may conclude that R_P of a primary parallel compensated IPT converter is smaller than that of a primary series compensated IPT converter. Similarly, we have $R_{PP} \approx R_{PPS}$ and $\frac{R_{SPP}}{R_{SPS}} \approx \left(\frac{\gamma_{PP}}{\gamma_{PS}}\right)^2 = 0.6669$. Likewise, we may conclude that R_S of a secondary parallel compensated IPT converter is smaller than that of a secondary series compensated IPT converter. So, in general, parallel compensation has better efficiency than series compensation.

Comparing maximum efficiencies at an identical power output of the SP and PS IPT converters, due to the lower output voltage of the PS IPT converter, the near constant diode drop loss is more significant at lower voltage output. Thus, the maximum efficiency of the SP IPT converter is better than the PS IPT converter. As a result, the maximum efficiency points are ordered from highest to lowest for IPT converters with compensations PP, PS, SP and SS as shown in Fig. 9.

C. Input and Output Currents and Maximum Efficiency Points of the Four Basic IPT Converters

Figs. 10(a) and 10(b) show the measured input current I_1 and the output current I_2 of the four basic IPT converters at maximum efficiency points. They agree with the analysis in Section IV, i.e., primary series compensation leads to a higher input current, and secondary series compensation leads to a higher output current at maximum efficiency point.

D. Control for Optimized Efficiency in PP IPT System

Optimal efficiencies at static conditions have been measured in Section VI-A for the four basic IPT converters. A simple and fast control scheme has been developed for the SS IPT

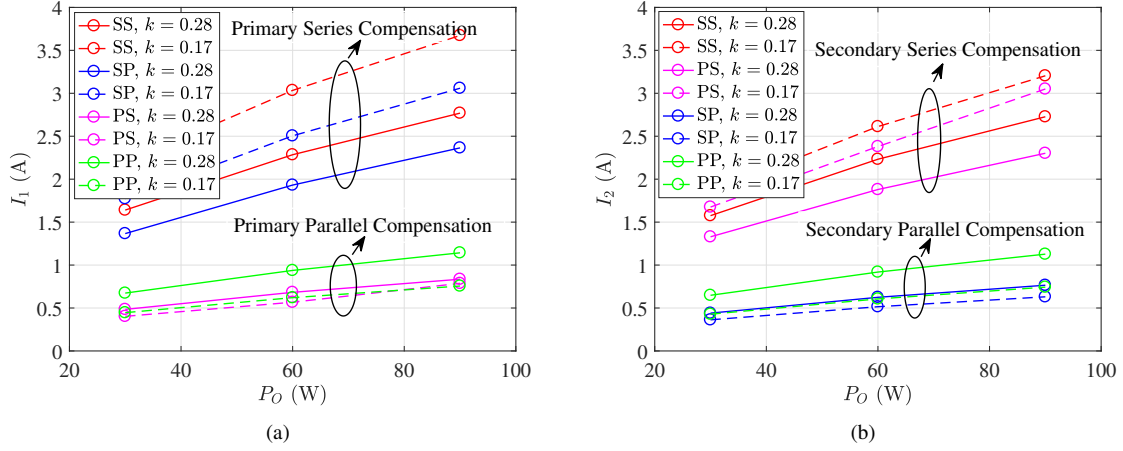


Fig. 10. (a) Measured input current I_1 and (b) measured output current I_2 of the four basic IPT converters at maximum power efficiency points.

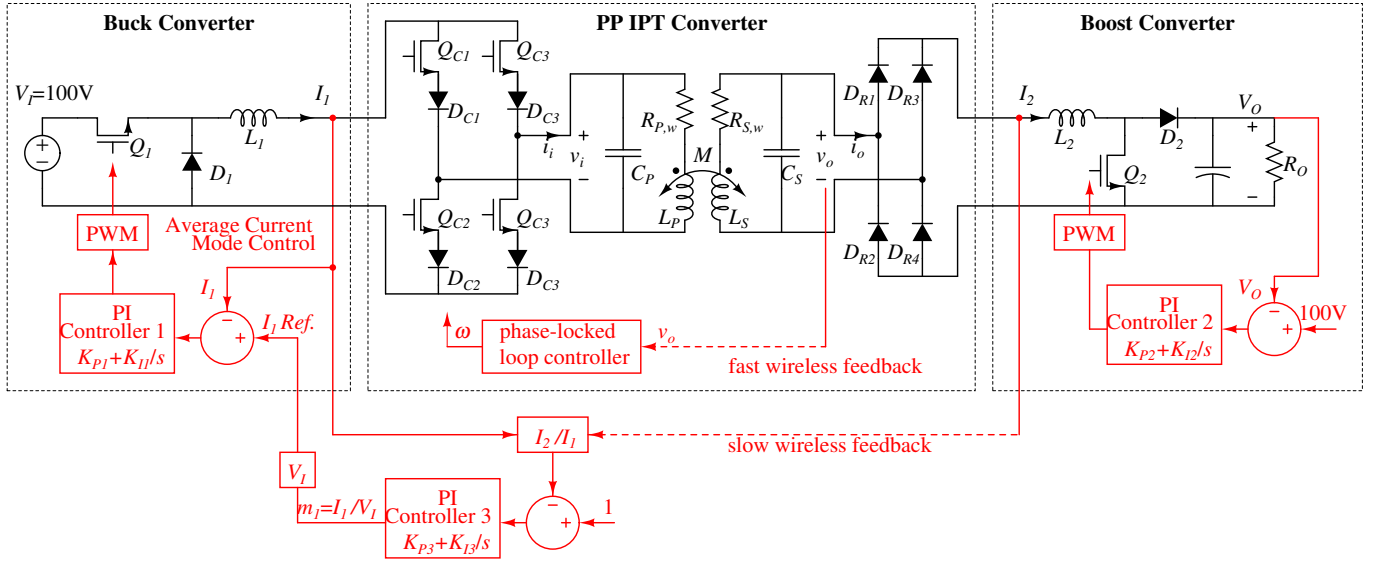


Fig. 11. Schematics and control diagrams of a multi-stage PP IPT system. Components: Q_1 and Q_2 are IPP60R165CP, D_1 and D_2 are MBRB2020CT. Parameters : $C_2 = 470 \mu\text{F}$, $L_1 = L_2 = 3.3 \text{ mH}$, $V_I = 100 \text{ V}$, $V_O = 100 \text{ V}$, $K_{P1} = 0.25$, $K_{I1} = 25$, $K_{P2} = 0.04$, $K_{I2} = 0.8$, $K_{P3} = 0.02$, $K_{I3} = 0.08$.

converter which does not need adaptive compensation and frequency tracking [24]. In Section VI-B, we have shown that the PP IPT converter has the highest efficiency. This converter is therefore selected in this paper for the experimental verification of the linear control scheme. A multi-stage system is constructed with schematics shown in Fig. 11, where the PP IPT converter is connected with a front-end buck converter and a load-side boost converter. A photo of the experimental setup is shown in Fig. 8.

Inside the PP IPT converter, the phase of AC voltage v_o is detected and transmitted wirelessly from the secondary to the primary via fast wireless feedback method, i.e., infrared emitter and receiver [29]. A PLL is implemented to control the operating frequency against the variation of k . Thus the PP IPT converter operates at LIV with ZPA and behaves as a transresistance converter. For the front-end buck converter, current-mode control is used to program the inductor current which

drives the PP IPT converter. The load-side boost converter is driven by the output voltage of the PP IPT converter and regulated by a standalone PI controller to generate a constant dc voltage output V_O . Currents I_1 and I_2 of the PP IPT converter are sampled. I_2 can be transmitted wirelessly from the secondary to the primary via a slow wireless feedback method, i.e., 2.4G. According to the experimental measurements shown in Fig. 9(d), $I_2/I_1 \approx 1$ can be selected as control reference to achieve the optimized efficiency. A PI controller is used to control the transfer function $H(R_L) = I_2/I_1$.

With PLL control, the dynamic response of the operating frequency against the variation of k is recorded as shown in Fig. 12(a). Typical experimental waveforms of the PP IPT converter are shown in Fig. 12(b). Voltage v_o measured before the rectifier circuit of the IPT converter is kept lagging behind i_i with a phase angle of $\frac{\pi}{2}$.

Transient waveforms of I_1 and I_2 using a linear controller

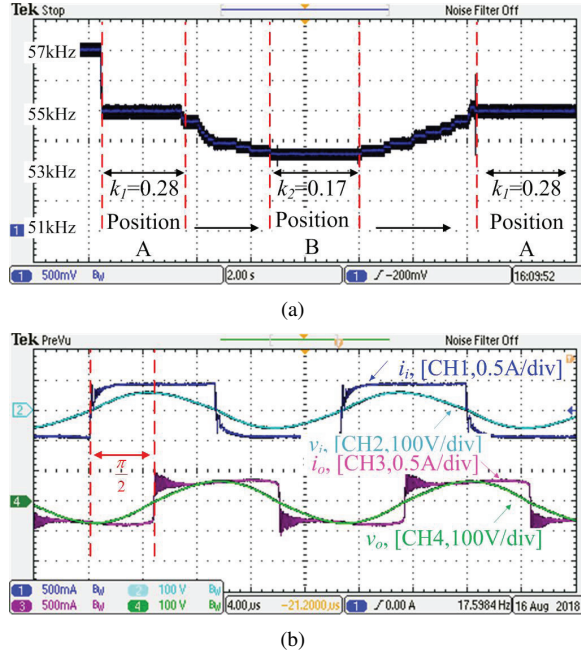


Fig. 12. (a) Reponse of the operating frequency when k dynamically changes from $k_1 = 0.28$ (position A) to $k_2 = 0.17$ (position B) and from $k_2 = 0.17$ (position B) back to $k_1 = 0.28$ (position A). (b) Experimental waveforms of PP IPT converter.

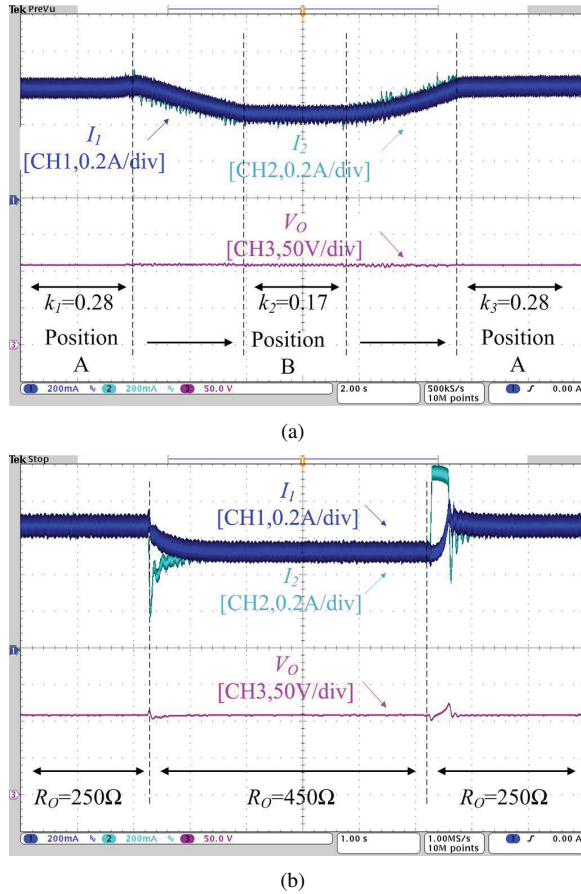


Fig. 13. Transient waveforms of I_1 , I_2 and V_O for (a) k dynamically changing from $k_1 = 0.28$ (position A) to $k_2 = 0.17$ (position B) and from $k_2 = 0.17$ (position B) back to $k_1 = 0.28$ (position A), at the loading condition $R_O = 300 \Omega$. (b) R_O step changing from 250 to 450 Ω and from 450 to 250 Ω at $k = 0.28$.

for dynamic variations of k and load are shown in Fig. 13(a) and Fig. 13(b), respectively. The efficiency of the system is kept at its optimized value by observing that the instantaneous currents I_1 and I_2 are kept almost identical. Using the PI controller, the steady-state error is almost eliminated. In comparison to the control of the SS IPT converter, the linear control for the PP IPT converter in this paper needs specifically more control loops for the input current and frequency tracking. Thus, the overall controller speed is slower.

VII. CONCLUSION

A general linear control scheme for all four basic IPT systems to track the optimum efficiency point and independently regulate the output power is proposed in this paper. To facilitate the control, an additional control of either frequency or adaptive compensation is identified and formulated for the series-parallel, parallel-series and parallel-parallel (PP) IPT converters against the variation of coupling coefficient (k). Control references of the k - and load-independent transfer functions are derived for all the four basic IPT converters for the fast linear control. The maximum efficiencies of four basic IPT systems are analyzed, compared and verified theoretically and experimentally. It is found that the maximum efficiencies of the four basic IPT systems are in decreasing order given by parallel-parallel, series-parallel, parallel-series and series-series compensated IPT converters. The linear control scheme with additional frequency control in conjunction with optimum efficiency tracking and independent load regulation is validated experimentally using an efficient PP IPT converter system.

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